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Extracting the global signal from 21-cm fluctuations: the multitracers approach

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ABSTRACT

The multitracers technique employs a ratio of densities of two differently biased galaxy samples that trace the same underlying matter density field, and was proposed to alleviate the cosmic variance problem. Here, we propose a novel application of this approach, applying it to two different tracers one of which is the 21-cm signal of neutral hydrogen from the epochs of reionization and cosmic dawn. The second tracer is assumed to be a sample of high-redshift galaxies, but the approach can be generalized and applied to other high-redshift tracers. We show that the anisotropy of the ratio of the two density fields can be used to measure the sky-averaged 21-cm signal, probe the spectral energy distribution of radiative sources that drive this signal, and extract large-scale properties of the second tracer, e.g. the galaxy bias. Using simulated 21-cm maps and mock galaxy samples, we find that the method works well for an idealized galaxy survey. However, in the case of a more realistic galaxy survey that only probes highly biased luminous galaxies, the inevitable Poisson noise makes the reconstruction far more challenging. This difficulty can be mitigated with the greater sensitivity of future telescopes along with larger survey volumes.

Key words: galaxies: high redshift – cosmology: theory – dark ages, reionization, first stars.

1 INTRODUCTION

The exploration of the first billion years of cosmic history is under way: observations of lensed fields with the *Hubble Space Telescope* (*HST*) have revealed bright galaxies at the onset of the Epoch of Reionization (EoR; $z \sim 6$ –10) with the most distant galaxy detected at redshift $z \sim 11.1$ (Oesch et al. 2016); the Atacama Large Millimeter Array (ALMA) sees dusty bright galaxies at $z \sim 9$ (e.g. Hashimoto et al. 2018); while high-redshift quasars have been seen above redshift 7 (the highest redshift quasar was found at $z = 7.54$, Bañados et al. 2018). Existence of such massive and metal-rich objects when the Universe was less than a billion years old suggests an early formation of the first stars (e.g. as early as $z \sim 15$ in the case of the metal-rich galaxy at $z = 9.1$; Hashimoto et al. 2018).

According to theory, the first stars turn on at $z \sim 30$ –60 (e.g. Naoz, Noter & Barkana 2006; Bromm 2017). This hypothesis can be tested with the next-generation instruments designed to observe the high-redshift Universe at different wavelengths. Some examples include the effort in X-rays such as *Lynx* (Gaskin et al. 2018), which is predicted to have enough sensitivity to see accreting black holes of mass $10^4 M_\odot$ at $z \sim 10$, and infrared telescopes such as the

James Webb Space Telescope (*JWST*; which should have enough sensitivity to see galaxies out to redshift ~ 16 , Cowley et al. 2018). However, these telescopes will have small fields of view and will mainly yield deep observations of small patches of the sky. Intensity mapping of molecular lines is another promising technique to probe the typical population of high-redshift star-forming galaxies, allowing us to survey large cosmic volumes (e.g. Kovetz et al. 2017; Moradinezhad & Keating 2018; Moradinezhad, Keating & Fialkov 2019).

The 21-cm signal produced by neutral hydrogen atoms in the intergalactic medium (IGM) is predicted to be a powerful probe of the early Universe at $z \gtrsim 6$ and is complementary to the direct observations of bright sources (see Barkana 2016 for a recent review of the 21-cm line). The brightness temperature of the 21-cm line is driven by the thermal and ionization histories of the gas as well as by the Ly α radiation of the first stars (Wouthuysen–Field effect; Wouthuysen 1952; Field 1958).

The sky-averaged (global) 21-cm signal contains information on the evolution history of the Universe. The timing of cosmic events such as the formation of the first population of stars, the onset of cosmic heating by the first population of X-ray sources, and the beginning of reionization are imprinted in the shape of the global signal (e.g. Cohen et al. 2017). Owing to the high expected scientific gains, several pioneering instruments are aspiring to observe the all-

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sky radio spectrum (Bowman & Rogers 2010; Voytek et al. 2014; Singh et al. 2018a; Philip et al. 2018; Price et al. 2018). Recently, the EDGES team has claimed discovery of the cosmological signal from redshifts $z \sim 14$ –26. An absorption trough with amplitude close to 500 mK (three times deeper than expected in standard astrophysical scenarios) centred at 78 MHz was measured with EDGES low-band instruments (Bowman et al. 2018a). If confirmed,¹ this signal is the first observational evidence of primordial star formation at the dawn of the Universe when it was only 200 million years old. At lower redshifts, attempts to observe the global signal have so far yielded non-detection, placing limits on the astrophysical parameter space (Monsalve et al. 2017, 2018, 2019; Singh et al. 2017, 2018b).

Fluctuations in the 21-cm field are complementary to the global signal, containing far more information on the distribution of radiative sources as well as on the characteristic scales on which these sources affect the environment. The latter can be related to the typical wavelength of the emitted photons, making the fluctuations a sensitive probe of the nature of the first stars and black holes (e.g. Fialkov, Barkana & Visbal 2014; Fialkov & Barkana 2014). The first attempt to detect fluctuations in the 21-cm signal via the redshifted 21-cm line at 151 MHz dates back to 1986 and targeted gaseous pancakes at $z \sim 8$ (Bebington 1986). At present, interferometric arrays are targeting fluctuations of the signal from the EoR as well as from the earlier epoch of cosmic dawn, yielding upper limits (e.g. Paciga et al. 2013; Beardsley et al. 2016; Patil et al. 2017; Gehlot et al. 2018; Eastwood et al. 2019). Although at present these limits are too weak to have interesting astrophysical implications, the effort is ongoing. Dedicated experiments such as the Hydrogen Epoch of Reionization Array (DeBoer et al. 2017) and facilities such as NenuFAR (Zarka et al. 2012) and the Square Kilometer Array (SKA; Koopmans et al. 2015) will measure the 21-cm fluctuations from cosmic dawn and the EoR over a wide range of scales.

Expected correlations between the features of the global signal and the details of the power spectrum (Cohen, Fialkov & Barkana 2018) suggest that the power spectrum measurements could be used to infer the global history of the Universe. Extracting the global signal directly from the interferometric measurements of the power spectrum has been discussed in the literature (Presley, Liu & Parsons 2015; Singh et al. 2015; Venumadhav et al. 2016; McKinley et al. 2018). However, such observations are particularly challenging because, in order to extract the global signal from the visibilities, one needs to characterize the antenna cross-talk and the correlated thermal noise to high precision (Bernardi, McQuinn & Greenhill 2015; Presley et al. 2015; Singh et al. 2015; Venumadhav et al. 2016). In this paper, we propose an alternative method to measure the global signal from the 21-cm fluctuations using the multitracer approach. The paper is organized as follows. In Section 2, we briefly summarize the standard multitracer technique (Seljak 2009). The physics of the 21-cm line, as well as the simulations used to generate the 21-cm signals and the galaxy fields, are described in Section 3. We summarize the parameter extraction algorithm in Section 4. The results are reported in Section 5. Finally, we conclude in Section 6. Throughout the paper, we assume standard Λ CDM cosmology with the values of cosmological parameters measured by the *Planck* satellite (Planck Collaboration XLVI 2016). All distances are calculated in comoving Mpc and wavenumbers in comoving Mpc^{-1} . Because in this paper we are mainly interested

in illustrating a new technique and are predominantly focusing on low redshifts ($6 \lesssim z \lesssim 15$), we do not address the EDGES-Low observation and only consider standard astrophysical models (e.g. as is summarized in Cohen et al. 2017). However, if the EDGES detection is confirmed, the unusually strong global 21-cm signal would imply enhanced fluctuations (e.g. Fialkov, Barkana & Cohen 2018; Fialkov & Barkana 2019) and make the proposed measurement much more feasible.

2 MULTITRACER TECHNIQUE

Originally introduced to compensate for the cosmic variance in large-scale structure galaxy surveys (Seljak 2009), the multitracer method employs a ratio of the density fields of two different populations of galaxies, $\delta_{\text{gal}}(\mathbf{k}, z)$, tracing the same underlying large-scale matter density field, $\delta(\mathbf{k}, z)$. In the linear regime, the relationship between the galaxy and matter density fields in Fourier space is

$$\delta_{\text{gal}}(\mathbf{k}, z) = (b + \mu_k^2 f) \delta(\mathbf{k}, z), \quad (1)$$

where \mathbf{k} is the comoving wavenumber, b is the bias of the galaxy field, $\mu_k = \cos \theta_k$ is the cosine of the angle θ_k with respect to the line of sight, and the factor $f = d \ln D / d \ln (1+z)^{-1}$ measures the growth of structure and is close to unity at the redshifts of interest ($6 \lesssim z \lesssim 30$) where the universe is matter dominated. In equation (1), the angular dependence is introduced by the Kaiser effect (Kaiser 1987). Because the two galaxy populations sample the same underlying density field, the ratio of the Fourier transforms of their densities is independent of $\delta(\mathbf{k}, z)$, and for every μ_k it is fully determined by the galaxy biases (and the factor f). Therefore, the ratio does not suffer from cosmic variance and allows access to information on the largest observable scales where the number of samples is small. This method has been shown to improve the constraints on non-Gaussianity of the initial conditions from inflation (Seljak 2009), redshift space distortions (McDonald & Seljak 2009), general-relativistic effects in the observed density of sources (Alonso & Ferreira 2015).

In this paper, we develop a new application of the multitracer method by replacing one of the tracers by simulated fluctuations in the 21-cm signal, $\delta_{21}(\mathbf{k}, z)$. The resulting ratio of the density fields is deterministic and anisotropic. We show that the angular dependence of the ratio can be used to extract the global 21-cm signal, galaxy bias and spectral properties of the first X-ray sources.

3 SIMULATED DATA

3.1 21-cm signal

The temporal evolution of the real-space three-dimensional differential brightness temperature of the 21-cm signal seen against the cosmic microwave background (CMB) radiation at low radio frequencies is given by

$$T_{21}(\mathbf{x}, z) = \frac{T_S - T_{\text{CMB}}}{1+z} [1 - \exp^{-\tau_{21}}], \quad (2)$$

where \mathbf{x} is the comoving coordinate, T_S is the spin temperature of the 21-cm transition (e.g. Barkana 2016, and references therein), $T_{\text{CMB}} = 2.725(1+z)$ K is the CMB temperature at redshift z , and τ_{21} is the 21-cm optical depth given by

$$\tau_{21} = \frac{3h_{\text{pl}} A_{10} c \lambda_{21}^2 n_{\text{H I}}}{32\pi k_B T_S (1+z) dv_r / dr}. \quad (3)$$

¹ Concerns were raised by Hills et al. (2018), which the EDGES team has addressed (Bowman et al. 2018b). Reanalysis of the integrated publicly available spectrum was also done by Singh & Subrahmanyan (2019).

Here, h_{pl} is Planck's constant, $A_{10} = 2.85 \times 10^{-15} \text{ s}^{-1}$ is the spontaneous emission coefficient, c is the speed of light, $\lambda_{21} = 21 \text{ cm}$ is the rest-frame wavelength of the signal, $n_{\text{H}1}$ is the number density of neutral hydrogen atoms that depends on the cosmological parameters and ionization history, k_{B} is the Boltzmann constant, and dv_r/dr is the radial component of the velocity gradient created by structure formation which (on average) equals $dv_r/dr = H(z)(1+z)^{-1}$ where $H(z)$ is the Hubble parameter. Throughout this paper, we assume that the 21-cm optical depth is small.

The spatially averaged $T_{21}(\mathbf{x}, z)$ gives the global 21-cm signal, $T_{21}(z)$. The density contrast in Fourier space, $\delta_{21}(\mathbf{k}, z)$, in mK units is the Fourier transform of $T_{21}(\mathbf{x}, z) - T_{21}(z)$.

3.1.1 Cosmic history

The dependence of $T_{21}(\mathbf{x}, z)$ on astrophysical parameters is encoded via their effects on the spin temperature and the ionization history. The variation of the 21-cm signal as a function of astrophysical parameters was recently explored by Cohen et al. (2017, 2019) who studied a large sample of 21-cm signals, with the key astrophysical parameters varied over the widest range allowed by existing observational and theoretical constraints.

In particular, Ly α radiation produced by the first stars couples the spin temperature to the kinetic temperature of the gas, T_K (Wouthuysen 1952; Field 1958). The exact timing of the Ly α coupling depends on the dominant regime of star formation (e.g. atomic cooling takes place in dark matter haloes above the mass threshold of $\sim 10^7 M_{\odot}$) as well as on the star formation efficiency, f_* . This process is very uncertain due to the lack of observations of high-redshift stars and is predicted to occur between $z \sim 35$ and $z \sim 12$ (Cohen et al. 2018). At these early times, after the onset of star formation and prior to the build-up of the first population of X-ray sources, fluctuations in the 21-cm signal are predominantly driven by the non-uniform Ly α background (Barkana & Loeb 2005b; Cohen et al. 2018). The peak power of these fluctuations at $k = 0.1 \text{ Mpc}^{-1}$ falls in the range $z \sim 14\text{--}35$ (Cohen et al. 2018). As more and more stars form, the intensity of the Ly α flux rises and its effect on the 21-cm signal saturates, leading to a suppression of the power spectrum. Although in this paper we focus on the effect of X-ray sources and ionizing radiation (i.e. lower redshifts), the process of Ly α coupling is modelled self-consistently and our findings can be equally applied to the epoch of Ly α coupling.

At the dawn of star formation intergalactic neutral gas is much colder than the CMB as a result of the cosmic expansion and due to the lack of significant X-ray heating. Therefore, the 21-cm signal is expected to be seen in absorption against the background. As soon as the first X-ray sources emerge, they heat up the gas in a non-uniform way. The heating transition (occurring at redshift z_h) marks the moment when the 21-cm signal vanishes as a result of the average gas temperature nearing that of the background radiation. At redshifts lower than z_h , the 21-cm signal is observed in emission. According to the parameter study by Cohen et al. (2018), z_h is lower than 22 for all the explored scenarios. In some models, X-ray heating is never strong enough to heat the gas above T_{CMB} . Non-uniform heating leads to a boost in power of the 21-cm fluctuations (Pritchard & Furlanetto 2018) and is the primary source of fluctuations at $z \sim 9\text{--}24$ (Cohen et al. 2018). Properties of X-ray sources, such as their bolometric luminosity and spectral energy distribution (SED), affect the heating process, and, therefore, can be extracted from the 21-cm signal. In particular, in Fialkov et al. (2014) and Fialkov & Barkana (2014), we compared the effect of a

realistic SED of X-ray binaries (a relatively hard spectrum peaking at $\sim 2 \text{ keV}$, Fragos et al. 2013) to the heating by softer sources. We found that hard sources are less efficient in heating up the gas, which results in a deeper absorption trough, lower emission peak and lower z_h . The SED has a strong effect on fluctuations: the power is suppressed on scales smaller than the mean free path of X-ray photons. In the case of the soft SED, the mean free path is short and most of the injected energy is absorbed close to the sources, while in the case of the hard sources heating is distributed over a larger range of scales.

The effect of X-rays on the 21-cm signal saturates once the gas temperature exceeds that of the CMB, and at later times the 21-cm signal is driven mostly by the reionization history. The process of reionization dominates the low-redshift regime, with the fluctuations peaking at $z < 13$ (again, the exact timing is very model dependent, Cohen et al. 2018). According to the existing observations of quasars, Ly α emitters, Lyman-break galaxies, and the CMB optical depth, reionization ends at $z_{\text{eor}} \sim 6$ or later (McGreer, Mesinger & D'Odorico 2015; Greig et al. 2017; Bañados et al. 2018; Mason et al. 2018; Planck Collaboration VI 2018; Weinberger, Haehnelt & Kulkarni 2019) and the 21-cm signal from the IGM essentially vanishes at that redshift.

3.1.2 Simulations

Three-dimensional realizations of the evolving 21-cm signal are generated using hybrid simulations (e.g. Fialkov et al. 2014; Cohen et al. 2017) inspired by Mesinger, Furlanetto & Cen (2011). The simulations were initiated at $z = 60$, at which the real-space density field $\delta(\mathbf{x}, z)$ was seeded with the resolution of three comoving Mpc, and evolved down to $z = 6$. The density fluctuations on the 3 Mpc scale are evolved linearly with redshift, while sub-grid models are used to account for processes occurring at unresolved scales, such as gravitational collapse and star formation. Abundance of dark matter haloes at each redshift and of each halo mass M_h is computed using the extended Press-Schechter formalism (Barkana & Loeb 2004). Each halo above the atomic cooling threshold is assumed to host a galaxy of stellar mass $M_* = f_* f_{\text{gas}} M_h$, where f_{gas} is the redshift-dependent fraction of the baryon density contained in haloes of mass M_h that also depends on the local value of the relative velocity between dark matter and gas (Tsaliakhovich, Barkana & Hirata 2011). We assume Population II star formation with star formation efficiency of $f_* = 5$ per cent (see e.g. Mirocha, Furlanetto & Sun 2017; Mirocha & Furlanetto 2019, for alternative galaxy models used in other 21-cm studies). Radiative backgrounds produced by stars and their remnants are calculated accounting for inhomogeneity and light-cone effects. Reionization is modelled using the excursion set formalism (Furlanetto, Zaldarriaga & Hernquist 2004). Finally, using the calculated inhomogeneous time-dependent fields (density, X-ray, and Ly α backgrounds) as well as reionization history, the evolution of the redshifted isotropic 21-cm signal is followed according to equation (2) in the limit of small optical depth. Peculiar velocity effects are added in the post-processing stage as described in Section 3.1.3.

Our results are shown for three combinations of reionization and heating parameters (identical to what we explored in Fialkov, Barkana & Cohen 2015):

- (i) Case 1: Late EoR ($\tau = 0.067$, $z_{\text{eor}} \sim 6.5$) and soft X-ray SED. The redshift of the heating transition in this case is $z_h = 14.5$.
- (ii) Case 2: Late EoR ($\tau = 0.067$, $z_{\text{eor}} \sim 6.5$) and hard X-ray SED with $z_h = 12.1$.

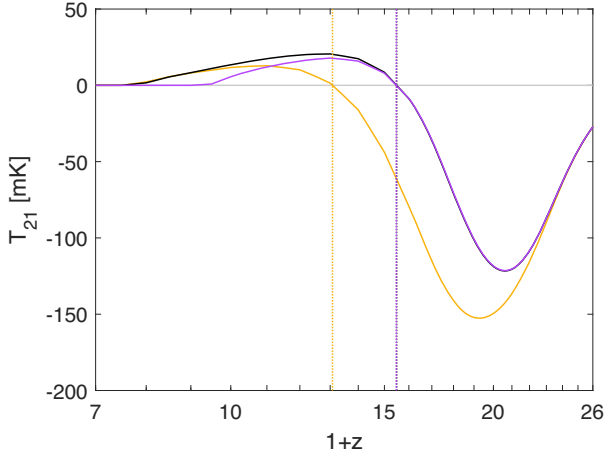


Figure 1. Simulated global 21-cm signals for Case 1 (black), Case 2 (orange), and Case 3 (purple). Vertical dotted lines show the redshifts of the heating transition. Horizontal dotted line shows marks $T_{21} = 0$ for reference.

(iii) Case 3: Early EoR ($\tau = 0.085$, $z_{\text{eor}} \sim 8$) and soft X-rays yielding $z_h = 14.5$.

All cases assume an identical X-ray bolometric luminosity per star formation rate of $3 \times 10^{40} \text{ erg s}^{-1} \text{ M}_{\odot}^{-1} \text{ yr}$.

The corresponding 21-cm global signals are shown in Fig. 1 (solid lines). As expected, at high redshifts the signals 1 and 3 coincide because of the identical X-ray heating, differing only at lower redshifts when reionization becomes important. On the contrary, signals 1 and 2 are identical at low redshifts and differ at high z . This is because Cases 1 and 2 have identical reionization histories but different X-ray heating, and at low- z X-ray heating is saturated and does not play a role. The absorption trough is much deeper in Case 2 compared to Cases 1 and 3 because hard X-ray sources are less efficient in heating the IGM than the soft sources (e.g. Fialkov et al. 2014).

Using the specifications of future facilities (such as the SKA²) as an indication, we employ cosmological simulations of 768 Mpc on a side with 3 Mpc resolution, which give access to fluctuations on scales $\sim 0.01\text{--}1 \text{ Mpc}^{-1}$. We also use smaller simulations of 384³ Mpc³ to explore scaling of the statistical errors with the survey volume (see discussion in Section 4).

3.1.3 Anisotropy

To the leading order, the 21-cm signal (equation 2) is isotropic and depends on the evolving distribution of star forming haloes convolved with the spherically symmetric window functions, $W(x, z)$, which quantify the response of the signal to the radiative backgrounds (X-ray, UV, and Ly α ; Barkana & Loeb 2005a; Fialkov et al. 2015). In Fourier space and in the linear regime, the signal can be written as

$$\delta_{21}^{\text{iso}}(\mathbf{k}, z) = T_{21} W(k, z) \delta(\mathbf{k}, z), \quad (4)$$

where $W(k, z)$ is the Fourier transform of $W(x, z)$. We calculate the window function directly from the simulated data (prior to adding

the velocity effects) by averaging the ratio $T_{21}^{-1} \delta_{21}(\mathbf{k}, z) / \delta(\mathbf{k}, z)$ over the direction of \mathbf{k} and refer to it as the ‘theoretical’ window function.

The peculiar velocity field adds non-linearity, breaks the spherical symmetry, and results in an angular-dependent 21-cm signal. The non-linear anisotropic density contrast, $\delta_{21}^{\text{nonlin}}(\mathbf{k}, z)$, is calculated from the real space isotropic signal by multiplying it by the factor $(dv_r/dr)^{-1}$. Because on the scales explored with our simulations the peculiar velocities are small compared to the Hubble flow, this factor can be approximated by $H^{-1}(z)(1+z) [1 - \delta_{d_r v_r}(\mathbf{x}, z)]$ where $\delta_{d_r v_r}(\mathbf{x}, z)$ is the dimensionless velocity perturbation in real space calculated as the inverse Fourier transform of $\delta_{d_r v_r}(\mathbf{k}, z) = -\mu_k^2 \delta(\mathbf{k}, z)$ (Kaiser 1987; Bharadwaj & Ali 2004; Barkana & Loeb 2005a). This allows us to combine the linear peculiar velocity field with the other sources of 21-cm fluctuations in real space, non-linearly. In other words, the addition of the velocity field is non-linear even though its magnitude is calculated using linear theory (peculiar velocities are small compared to the Hubble flow, not compared to other perturbations). Finally, we take another Fourier transform in order to obtain the 21-cm fluctuation signal in k -space. We refer to this approach as our ‘non-linear’ case. As an illustration, in Fig. 2 we show power spectra for the astrophysical Case 1 at $z = 19$ (close to the redshift of the absorption trough). The Figure shows the spherically averaged isotropic power spectrum as a function of k (left) and the anisotropic two-dimensional power spectrum as a function of $k_{\text{par}} = \mu k$, projection of the wavenumber along the line of sight (more precisely, we plot the power spectrum as a function of the absolute value of k_{par}), and $k_{\text{perp}} = k \sqrt{1 - \mu^2}$, perpendicular to the line of sight.

It is useful to compare the non-linear case to the fully linearized version of the anisotropic 21-cm signal (e.g. Barkana & Loeb 2005a). In the linear regime, perturbations are additive and the anisotropic signal is given by

$$\delta_{21}^{\text{lin}}(\mathbf{k}, z) = \delta_{21}^{\text{iso}}(\mathbf{k}, z) - T_{21} \delta_{d_r v_r}(\mathbf{k}, z), \quad (5)$$

where the minus sign arises because the velocity term is in denominator (equation 3). We refer to this approach as the ‘linear’ case. In the linear regime $\delta_{21}^{\text{lin}}(\mathbf{k}, z)$ can also be written as $T_{21} [W(k, z) + \mu_k^2] \delta(\mathbf{k}, z)$. We will make use of this property in Section 4.

3.2 Galaxies

Our second tracer is a mock galaxy survey calculated using the same simulations that were used to generate the 21-cm signals. As described in Section 3.1.2, each halo of mass above the atomic cooling threshold hosts a galaxy with the stellar mass proportional to its halo mass. Therefore, the simulation readily provides a galaxy catalogue. The treatment is self-consistent in that the 21-cm signal and the mock galaxy survey are probing the same large-scale density field and the same realization of galaxies.

In order to illustrate the technique, we first consider a simplified (‘ideal’) survey where the galaxy density field is modelled as in equation (1), assuming a fixed galaxy bias, $b = 5$. In this case, the effective number of galaxies in each simulated real-space cell is not necessarily an integer, as it is set by the cosmic mean abundance modified with respect to the local value of the large-scale density field.

Next, we generate a simple approximation of a more realistic galaxy field. We use the minimum mass of observed star-forming haloes, M_{min} , as a proxy for telescope sensitivity. A low threshold, $M_{\text{min}} = 10^7 \text{ M}_{\odot}$, mimics observations with an extremely sensitive telescope that can detect faint high-redshift galaxies formed in

²SKA will have a large field of view of ~ 5 deg at 100 MHz, corresponding to ~ 823 comoving Mpc at $z = 9$.

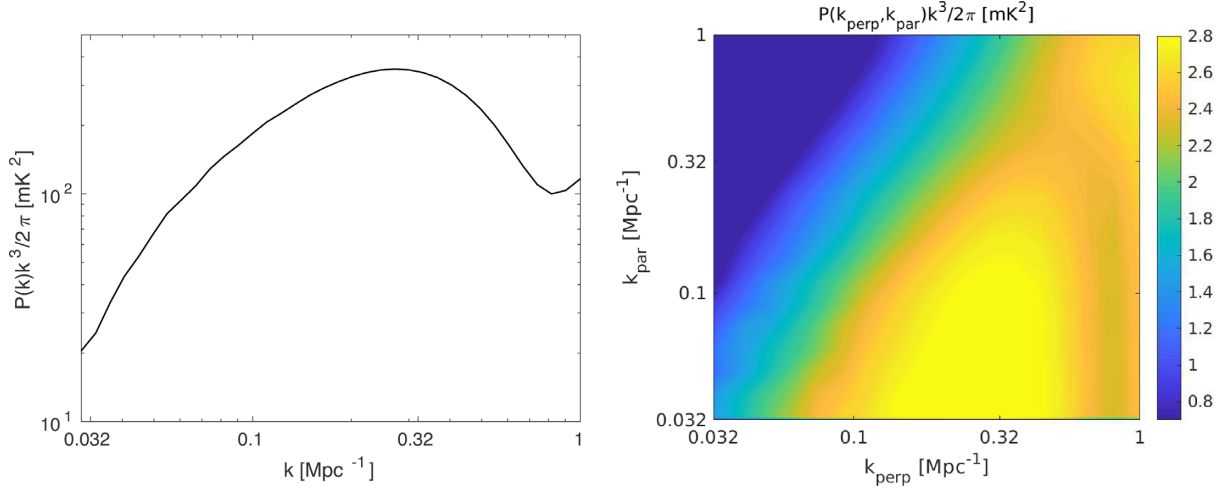


Figure 2. Power spectra of 21-cm fluctuations for Case 1 at $z = 19$. We show spherically averaged isotropic power spectrum versus k (left) and two-dimensional power spectrum as a function of $k_{\text{perp}} = k\sqrt{1 - \mu^2}$ and the absolute value of $k_{\text{par}} = \mu k$ (right). Colour code (see the colour bar on the right) corresponds to the logarithm (base 10) of the anisotropic power spectrum $P(k_{\text{perp}}, k_{\text{par}})k^3/2\pi$ in mK units. The velocity field was added non-linearly.

minihaloes. However, in reality such sensitive surveys will most likely probe only a small part of the sky. To make the multitracer analysis between galaxy surveys and the SKA (or similar) possible, large survey areas are required implying that the sensitivity will most likely be compromised. Therefore, we also consider higher values of $M_{\text{min}} = 10^8 M_{\odot}$ and $M_{\text{min}} = 10^9 M_{\odot}$. The minimum observable halo mass can be related to stellar mass (as described in Section 3.1.2). In the redshift range $z = 6$ – 15 and assuming cosmic mean value of the relative velocity between dark matter and gas, we find that $M_{\text{min}} = 10^8 M_{\odot}$ corresponds to $M_* \approx 7 \times 10^5 M_{\odot}$ and $M_{\text{min}} = 10^9 M_{\odot}$ corresponds to $M_* \approx 7 \times 10^6 M_{\odot}$. Relating the stellar masses directly to telescope sensitivity requires additional model for dust attenuation and is out of the scope of this paper.

To ensure that our galaxy distribution is realistic, we also make sure that the number of galaxies in any given cell, n_{cell} , is integer. We calculate n_{cell} by drawing it from a Poisson distribution with the mean value given by the mean expected number of galaxies³ $\bar{n}_{\text{cell}} = V_{\text{cell}} \langle n \rangle [1 + b(z)\delta_{\text{cell}}]$. Here, $V_{\text{cell}} = 27 \text{ Mpc}^3$ is the comoving volume of each cell in our simulation, $\langle n \rangle$ is the mean cosmic abundance of haloes above M_{min} , δ_{cell} is the mean overdensity of the cell, and $b(z)$ is the redshift-dependent galaxy bias which we calculate from the collapsed fraction, $b(z) = d\log f_{\text{coll}}(M_h > M_{\text{min}})/d\delta$. The noisy biased isotropic galaxy density field is, thus, $\delta_{\text{gal}}(\mathbf{x}, z) = n_{\text{cell}}[V_{\text{cell}} \langle n \rangle]^{-1} - 1$. Finally, anisotropy is added by applying the Kaiser effect as explained in Section 3.1.3 (in the linear case).

Examples of the cosmic mean number of haloes in a cell and the redshift-dependent galaxy bias $b(z)$ are shown in Fig. 3 as a function of redshift for several choices of M_{min} . The higher is the cut-off scale the lower is the number of star-forming haloes and the higher is the bias (although our calculated bias is somewhat higher than the measurements at $z \sim 6$, see Harikane et al. 2016; Hatfield et al. 2016). In contrast, the anisotropy term does not depend on the cut-off scale. Therefore, for higher M_{min} the anisotropy is effectively

weaker. This is the reason why (as we will see in Section 5.2) the method, which we explain in detail in Section 4, does not work for noisy galaxy samples with high M_{min} .

4 PARAMETER ESTIMATION

In this section, we show how the ratio of the two density fields, $\delta_{21}(\mathbf{k}, z)$ and $\delta_{\text{gal}}(\mathbf{k}, z)$, assuming an idealized galaxy survey, can be used to measure the global (sky-averaged) 21-cm signal, the window function and properties of the galaxy population (bias). Consider, first, the ratio in the linear regime

$$R_k^{\text{lin}}(z) \equiv \frac{\delta_{21}^{\text{lin}}(\mathbf{k}, z)}{\delta_{\text{gal}}(\mathbf{k}, z)}. \quad (6)$$

Because, as can be seen from equations (1) and (5), in the linear approximation both of these fields are proportional to $\delta(\mathbf{k}, z)$, its contribution cancels out and the ratio can be written as a deterministic function⁴ of $X \equiv \mu_k^2$ parametrized by $T_{21}(z)$, $W(k, z)$, and b

$$R_k^{\text{lin}}(z) = \frac{T_{21}(z) [W(k, z) + \mu_k^2]}{b + \mu_k^2}. \quad (7)$$

Here, we are only interested in high-redshift applications of the method ($6 < z < 26$, matter dominated universe) and set $f = 1$.

Our goal is to extract $T_{21}(z)$, $W(k, z)$, and b from the ratio of the simulated fields $\delta_{21}^{\text{lin}}(\mathbf{k}, z)$ and $\delta_{\text{gal}}(\mathbf{k}, z)$. To this end at every k and z , we bin the ratio into N_X bins along X , and fit it by a function of the form

$$F_k(X) = \frac{A_k + BX}{C + X}. \quad (8)$$

We measure the values of A_k , B , and C , which are then used to estimate the astrophysical quantities:

$$\hat{b} = C, \quad (9)$$

$$\hat{T}_{21}(z) = B, \quad (10)$$

³Importantly, the number of galaxies in each 3 Mpc cell is derived using the same statistics of collapsed objects that is used to calculate the 21-cm signal. This model is self-consistent in that the 21-cm signal and the mock galaxy survey are indeed probing the same realization of galaxies.

⁴More precisely, at every redshift equation (7) represents a set of N_k functions, where N_k is the number of samples of k .

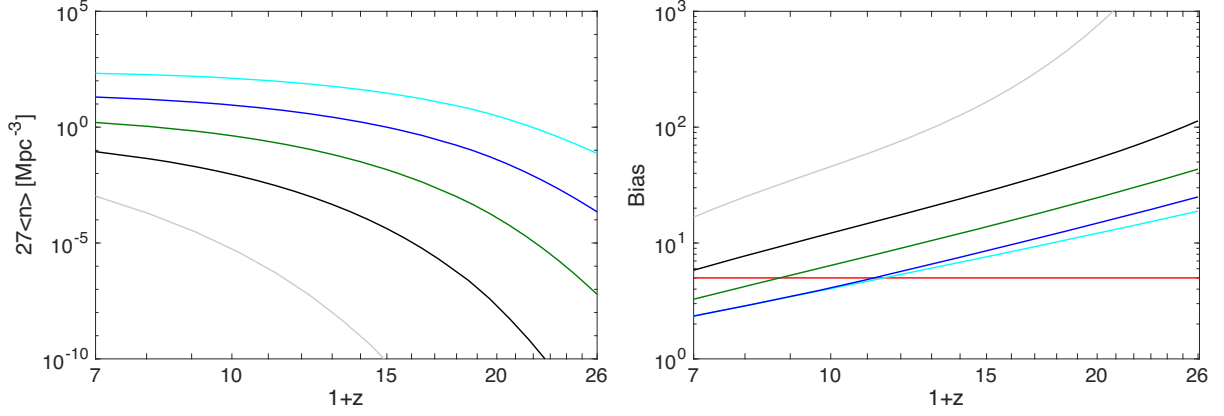


Figure 3. Left: Cosmic mean number of haloes in a cell, \bar{n}_{cell} . We consider $M_{\text{min}} = 10^7 M_{\odot}$ (cyan), $M_{\text{min}} = 10^8 M_{\odot}$ (blue), $M_{\text{min}} = 10^9 M_{\odot}$ (green), $M_{\text{min}} = 10^{10} M_{\odot}$ (black), $M_{\text{min}} = 10^{11} M_{\odot}$ (grey). Right: Redshift-dependent galaxy bias $b(z)$. The colour code is the same as in the left-hand panel. The scale-independent bias $b = 5$ (red horizontal line) is added for comparison.

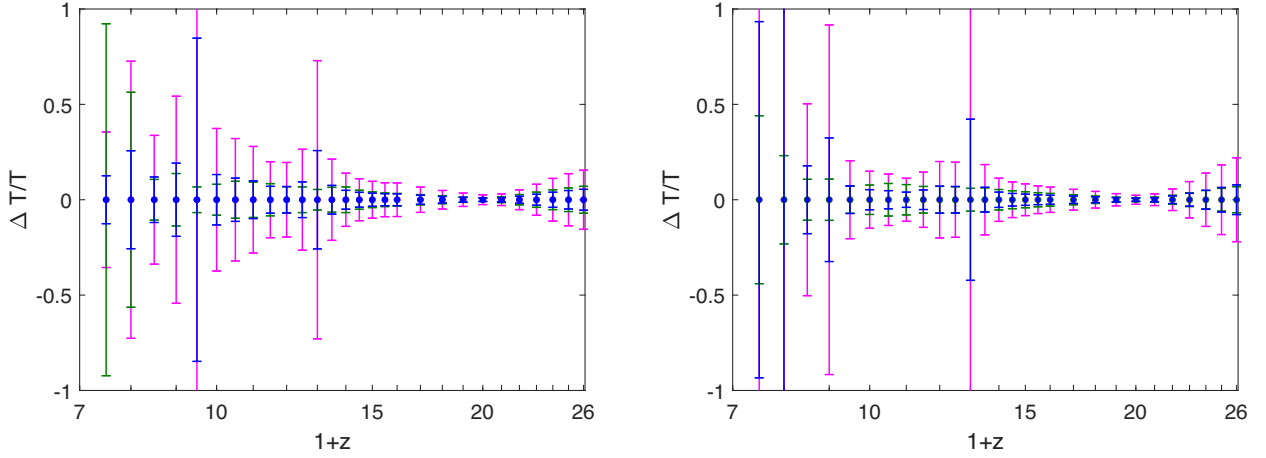


Figure 4. Statistical dimensionless errors in the brightness temperature ($\Delta T/T$) for boxes with 128^3 cells (Δ_{128} , magenta) and 256^3 cells (Δ_{256} , green). The scaled version $\tilde{\Delta}_{256} = \Delta_{128} (128/256)^{3/2}$ is also shown (blue). Left-hand and right-hand panels show the results drawn from different realizations of initial conditions. The results are shown for the astrophysical Case 2 for which the heating transition happens at $z = 12.1$ and assuming an idealized galaxy survey. We note that while this figure only shows statistical errors, Fig. 5 shows the systematic errors as well.

$$\hat{W}(k, z) = A_k/B. \quad (11)$$

At the end of this procedure (details are discussed in the Appendix), we have the best-fitting values of $\hat{b}(z)$, $\hat{T}_{21}(z)$, and $\hat{W}(k, z)$ together with $1 - \sigma$ statistical errors in each parameter (calculated using standard error propagation analysis). Note that without the anisotropic terms, only the degenerate combination $T_{21}(z)W(k, z)/b$ can be measured.

4.1 Accuracy

Our main results (discussed in Section 5) are derived from simulations of comoving volume 768^3 Mpc^3 (consisting of 256^3 cells). This volume is close to the projected field of view of the SKA, ~ 5 deg at 100 MHz, which at $z = 9$ corresponds to ~ 823 comoving Mpc. However, a few survey modes with the SKA are being discussed which would cover a larger area by surveying multiple fields of view, either 5 (deep), 50 (medium), or 500 (shallow) fields. Because simulating larger boxes than 768^3 Mpc^3 is not feasible at the moment, we explore the scaling of the results by down-

sizing the simulations. We compare with the results from smaller simulations of 384^3 Mpc^3 performed at the same resolution as the larger volumes. It is expected that, if the errors are dominated by statistical errors, decreasing the size of the simulated volume should degrade the parameter estimation. In this case, decreasing the number of statistically independent modes in the data cube from N^3 to M^3 is expected to increase the error by a factor of $(N/M)^{3/2}$. Our results closely follow this trend. The errors in the brightness temperature (i.e. the global 21-cm signal) as a function of redshift are demonstrated in Fig. 4 for two independent sets of initial conditions (left-hand and right-hand panels) for a box with 128^3 modes (Δ_{128} , magenta) and 256^3 modes (Δ_{256} , green); in addition, we show the scaled version of Δ_{128} multiplied by the numerical factor of $(128/256)^{3/2}$ ($\tilde{\Delta}_{256}$, blue). The value of Δ_{256} is very close to $\tilde{\Delta}_{256}$ at the majority of the considered redshifts indicating that the errors are of statistical origin at most redshifts. Therefore, the larger the survey, the more reliable reconstruction can be achieved. Comparing the right-hand and the left-hand panels we see that the size of the error bars only mildly depends on the specific realization of the initial density field. Provided that the fluctuations are detected with high enough significance,

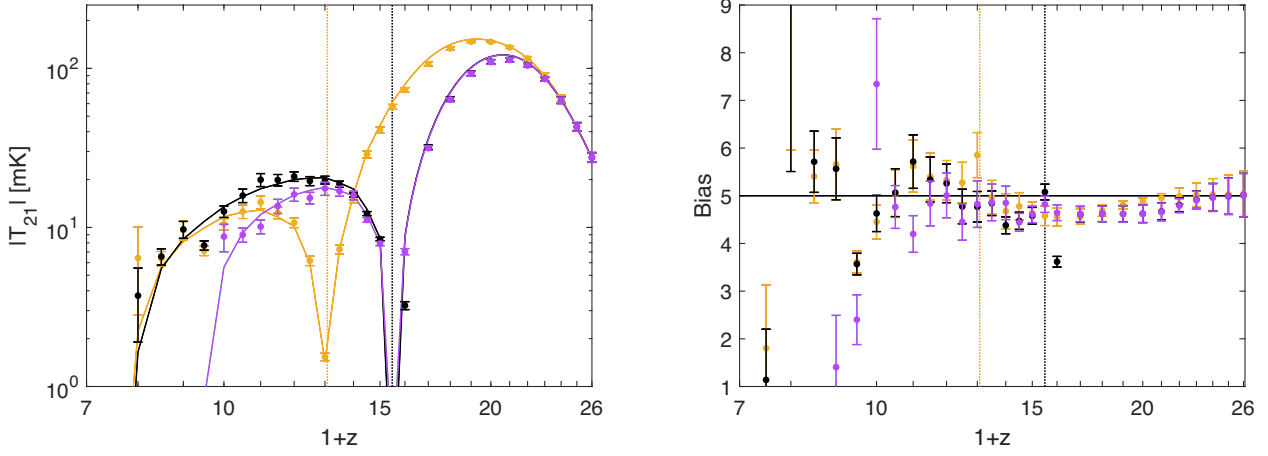


Figure 5. Left: The amplitude of the simulated global 21-cm signals (solid lines, log scale) and measured $|\hat{T}_{21}|$ (data points) extracted using the multitracer technique from the data with velocities added in real space (the non-linear case). We show Case 1 (black), Case 2 (orange), and Case 3 (purple). Each measurement is a result of fitting, extracted from one 768^3 Mpc 3 box, where no Poisson noise was added. The error bars indicate the 1σ error of non-linear regression calculated from the joint fitting of the temperature, window function, and bias. Vertical lines indicate the redshift of heating transition in each case. Right: Expected bias $b = 5$ (horizontal line) and measured bias \hat{b} (points) extracted using the multitracer technique. Same colour code as on the left.

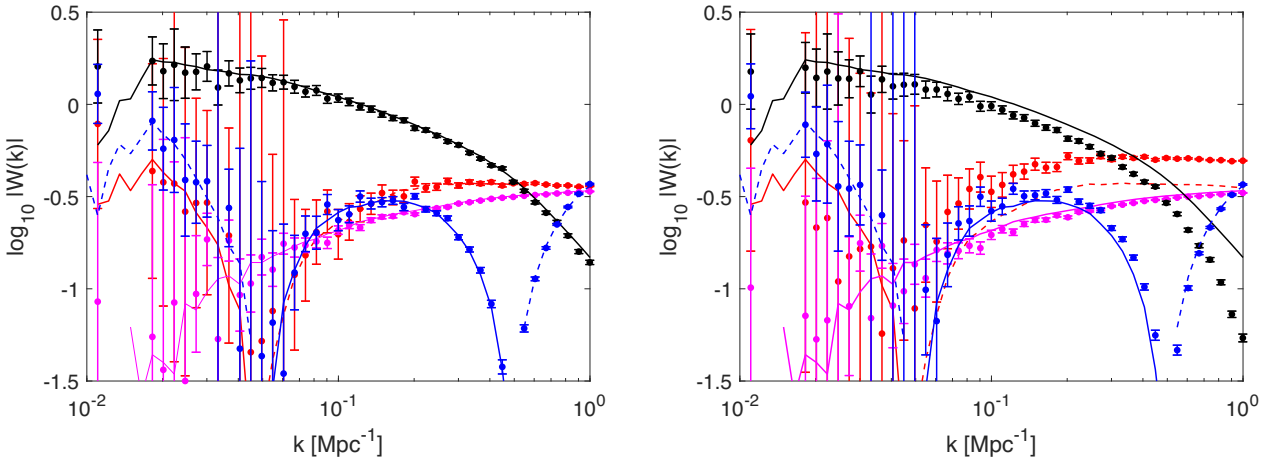


Figure 6. Logarithm (base 10) of the absolute value of the window function is shown as a function of wavenumber with in the linear (left) and non-linear (right) cases. The theoretical $W(k, z)$ is shown with solid (positive value) and dashed (negative value). Astrophysical models are shown for Cases 1 and 2 at the redshift of the global maximum/minimum of T_{21} : $z = 12/20$ for Case 1 (black/blue) and $z = 10/18$ for Case 2 (red/magenta). The reconstructed $\hat{W}(k, z)$ is marked with points of the corresponding colours. $\hat{W}(k, z)$ has the correct sign everywhere [matching $W(k, z)$]. We also show $1 - \sigma$ fitting error bars for each measurement.

we conclude that the SKA shallow survey should be the most effective survey for extracting the global 21-cm signal (assuming perfect extraction of the 21-cm field and that there exists a deep enough large-scale survey or another tracer to accompany the SKA measurement).

Statistical errors in galaxy bias and $W(k, z)$ (e.g. error bars in the right-hand panel of Fig. 5 and in Fig. 6) are also calculated via standard error propagation analysis. Because at each redshift the fitting is done simultaneously for all the $N_k + 2$ parameters – N_k samples of $W(k, z)$, and one sample of each b and $T_{21}(z)$ – the strength of the 21-cm signal affects measurement of the bias and the window function. The quality of the fit is poor (and statistical errors are high) for low amplitude signals, which includes the redshift of the heating transition at which $\hat{T}_{21}(z)$ is close to zero, and low redshifts where the signal vanishes due to reionization. On the other

hand, the fitting procedure performs well when the signal is strong, with the errors dropping to minimum at around $z \sim 20$ where the global signal reaches its maximum. Furthermore, for $W(k, z)$ the errors are larger at lower k modes (corresponding to larger spatial scales) because then the number of statistically independent modes is smaller. Quantitative discussion on the errors can be found in the next section.

In this paper, we assume perfect foreground removal/avoidance at wavenumbers between $k \sim 2\pi/[\text{box size}]$ (corresponding to the largest accessible scale) and 1 Mpc^{-1} . However, our method also works if the lowest modes are lost in the process of foreground subtraction. We test the robustness of the method by comparing the results obtained using wavenumbers in the $0.01\text{--}1 \text{ Mpc}^{-1}$ range and $0.05\text{--}1 \text{ Mpc}^{-1}$ range finding a very minor effect (see Fig. A1 in the Appendix).

5 RESULTS

Even though equation (8) was derived in the linear regime, here we use it to fit the ratio of the non-linear 21-cm field and an ideal (Section 5.1) as well as a realistic (Section 5.2) galaxy sample. As we will see below, the fitting procedure works well when equation (7) is a good representation of the data, i.e. when both the non-linearity and galaxy bias are small. The method is expected to perform poorly for highly biased galaxy sample or when non-linearity is strong. In these cases, systematic errors are expected.

5.1 Ideal galaxy surveys

Assuming an ideal galaxy survey, we extract the mean values and $1 - \sigma$ error bars of the brightness temperature and galaxy bias and show them in Fig. 5. Original values of these parameters [the global signal directly measured from the simulated field $T_{21}(\mathbf{x}, z)$ and the constant galaxy bias $b = 5$] are shown for comparison. The results are shown over a wide range of redshifts and for different sets of astrophysical parameters (Cases 1, 2, and 3 as discussed above).

As is evident from Figs 4 and 5, errors in the global signal are of the order of 10 percent at high redshifts where the signal is very strong and non-linearity is weak (9 percent at $z = 17$ for Case 1, including both the statistical error and the systematic offset). One exception is z_h . At this relatively high redshift, the global 21-cm signal is close to zero and the errors diverge. At lower redshifts, the reconstruction errors are higher (increasing to few tens percent, 21 per cent at $z = 8$ for Case1) because the non-linearity is strong and the signal is weak due to the ongoing reionization and saturated heating. Specifically, close to z_{eor} the errors are of the order of ~ 100 per cent as the 21-cm signal approaches zero, preventing efficient parameter estimation. As is evident from the left-hand panel of Fig. 5, throughout the cosmic history the errors in the reconstructed brightness temperature are much smaller than the variation of the signal introduced by the change in the astrophysical parameters (namely, X-ray SED and τ , both varied within margins allowed by existing observations). This indicates that the multitracers method could potentially yield constraints on the astrophysical parameters from the observed data, especially if wide-field surveys with the SKA are used. In a similar manner, the error in the galaxy bias (shown in the right-hand panel of Fig. 5) is of the order of 10 percent at high redshifts where the method works well (7 percent at $z = 17$ for Case 1, including both the statistical error and the systematic offset), increasing to few tens of percent at lower redshifts (~ 17 percent at $z = 8$ for Case 1).

The window function of the dominant radiative source can also be measured. The estimates of $\hat{W}(k, z)$ as a function of k are shown in Fig. 6 at two characteristic redshifts corresponding to the absorption trough of the 21-cm signal and the emission peak. The results are shown for the simulated Cases 1 and 2. We compare the expectation value $\hat{W}(k, z)$ with the theoretical value $W(k, z)$ computed using equation (4) where δ_{iso} is the isotropic density that we measured directly from our simulations (prior to adding the velocity effects). The results are shown for the linear (left-hand panel) and non-linear (right-hand panel) velocity perturbations.

In the case of linear theory, the reconstructed window function is in an excellent agreement with the theoretical curves for all the considered astrophysical scenarios and at all the explored redshifts. The errors are at sub-percent level at large k where the number of independent samples per bin is large. At lower k , the errors are much larger because of the small number of statistically independent

samples (showing that in this case we do not evade the cosmic variance problem).

In the non-linear case, equation (7) is not expected to be in a perfect agreement with the simulated data and degradation in the quality of the fit (equation 8) is expected. Nevertheless, there is a good agreement between the theory and the measurement at high redshifts where non-linearity is small, the effect of X-rays is the strongest and the signal itself ($|T_{21}|$) is the strongest. Specifically, at the redshift of deepest absorption (blue/magenta curve for Case1/2) both cases show a good agreement and small fitting errors at high k . The reconstruction is slightly better for the hard SED (Case 2) than for the soft SED (Case 1) owing to the ~ 30 percent deeper absorption trough. At lower redshifts, although the shape of the window function can still be recognized and the sign of $\hat{W}(k, z)$ is always correct [same as of $W(k, z)$], there is an offset between the theoretical and the measured window functions because the effect of X-rays is nearly saturated, non-linearity is large and the signal itself is low. For example, at the redshift of the emission peak (red and black lines in Fig. 6) the offset is above 50 per cent.

Around the heating transition (when temperature fluctuations dominate the 21-cm power spectrum), the slope of $W(k, z)$ is directly related to the hardness of the X-ray SED (Fialkov et al. 2015). If the spectrum is soft, heating happens predominantly on small spatial scales and the window function in the Fourier space is steep. On the other hand, energy is distributed over larger scales in the case of a hard SED and the window function is much flatter in the harmonic space. In Fig. 7, we demonstrate the variation of the window function with X-ray SED and find a good agreement with our earlier results (Fialkov et al. 2015). Therefore, if observed, the shape of $W(k, z)$ can be used to determine the SED of X-ray sources.

5.2 Realistic galaxy surveys

So far we have assumed an idealized galaxy survey. In this section, we consider a realistic galaxy survey with added Poisson fluctuations (see Section 3.2 for details) in the (more realistic) case of the non-linear velocity. The fitting procedure is the same as described in Section 4. The results are shown in Fig. 8 for $M_{\text{min}} = 10^8 M_{\odot}$ (purple) and $M_{\text{min}} = 10^9 M_{\odot}$ (orange) together with the ideal case (black) which is shown for comparison. The theoretical expectations are shown with solid curves. Note that the theoretical predictions for the bias depend on the minimum cut-off halo mass; while the theoretical curves for the global signal and the window function are independent of M_{min} .

The strong bias of bright galaxies makes the extraction of astrophysical parameters much more challenging, especially at high redshifts where these sources are extremely rare (as can be seen from Fig. 3 which shows the cosmic mean halo number in each cell as a function of redshift and for several choices of M_{min}). This is because in equation (7), if the bias is large, the anisotropic terms become relatively smaller and harder to measure. This effect combines with the larger Poisson noise of the rare galaxies. Although subject to large errors, the method still can be applied when M_{min} is low, e.g. $M_{\text{min}} = 10^8 M_{\odot}$. In this case, major features of $T_{21}(z)$, $b(z)$, and $W(k, z)$ can still be measured (purple data points in Fig. 8). For instance, although there is an offset between the theoretical and the measured window function, its shape is recognized correctly and the amplitude is within an order of magnitude of the theoretical value. The discrepancy is a few tens of percent in both the global signal and the redshift-dependence bias. However, the quality of the fit dramatically degrades as the cut-off mass is increased. Increasing M_{min} by just an order of magnitude greatly weakens the anisotropy

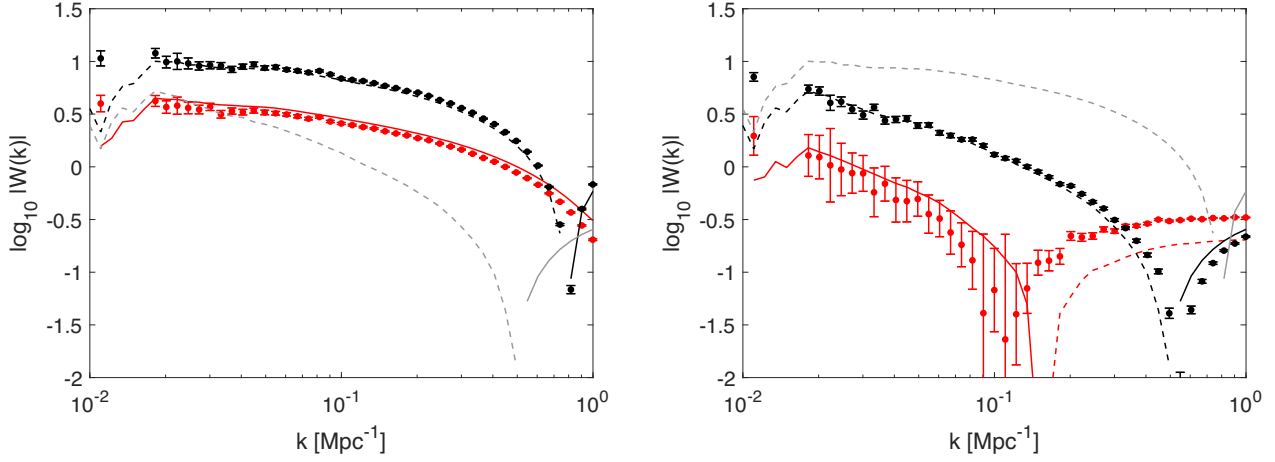


Figure 7. We compare the window function $\hat{W}(k, z)$ (logarithm, base 10, of the absolute value is shown) measured in the non-linear case (data points) to the theoretical window function $W(k, z)$ (curves) around the heating transition for Case 1 (soft X-ray SED, left) and Case 2 (hard X-ray SED, right). Solid lines show the positive value of $W(k, z)$, dashed – negative value. The fitted $\hat{W}(k, z)$ points have the correct signs [matching the $W(k, z)$ curves] in every case. The data are shown at $z_h - 1.5$ (red), $z_h + 1.5$ (black). The grey curves on each panel show the highest redshift curve from the opposite panel.

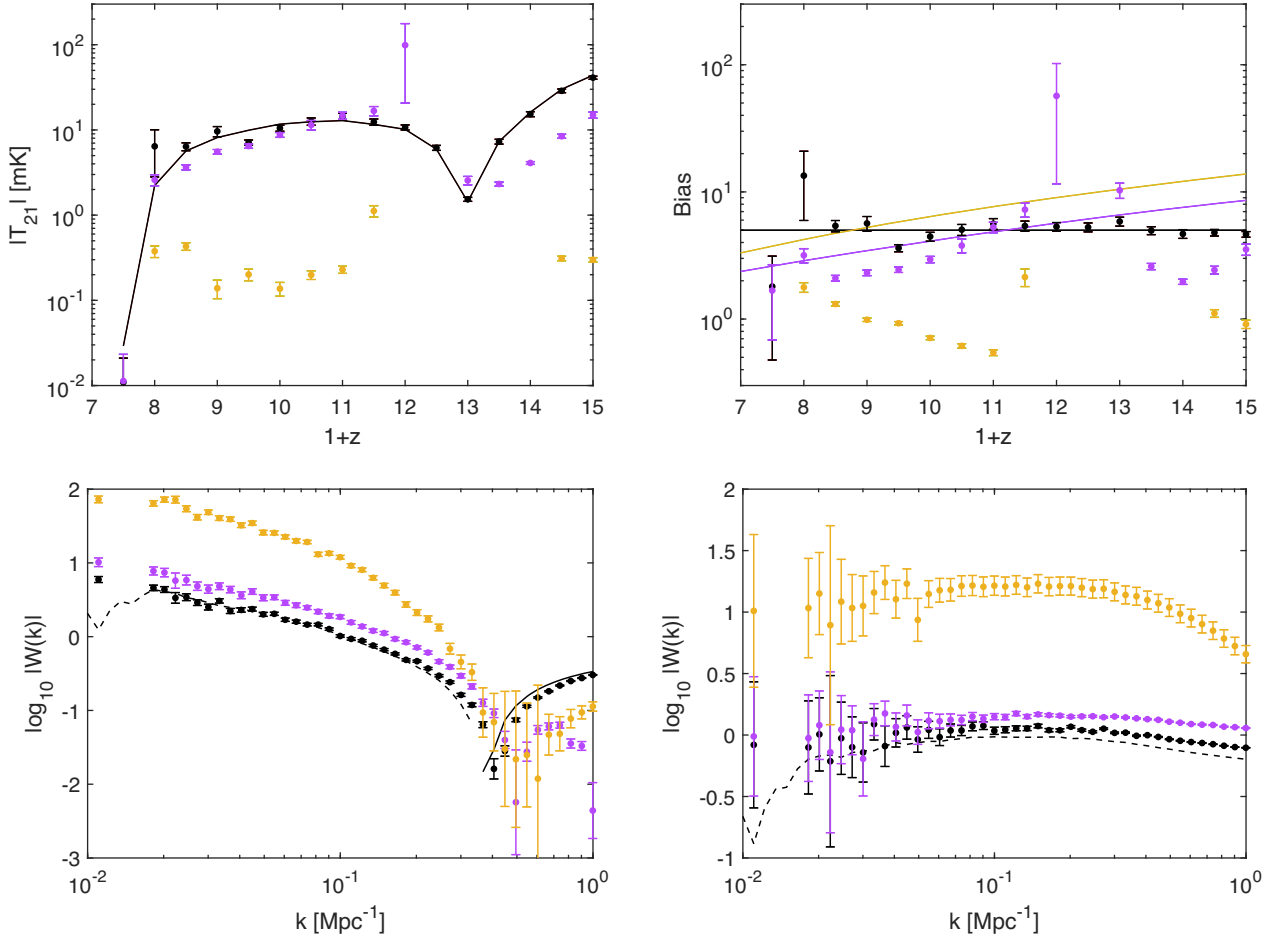


Figure 8. Top left: Global signal without Poisson noise (black) and with Poisson noise for the cut-off masses of $M_{\min} = 10^8 M_{\odot}$ (purple) and $M_{\min} = 10^9 M_{\odot}$ (orange). Top right: Galaxy bias, same colour code as on the left-hand side. In the ideal case the theoretical bias is $b = 5$, in the cases with Poisson noise we incorporate the redshift-dependent bias $b(z)$. Bottom: $\hat{W}(k, z)$ (data points) at $z = 14$ (left) and $z = 9$ (right) without (black) and with (purple and orange) Poisson noise. Curves mark $W(k, z)$ [solid/dashed lines correspond to the positive/negative values of $W(k, z)$].

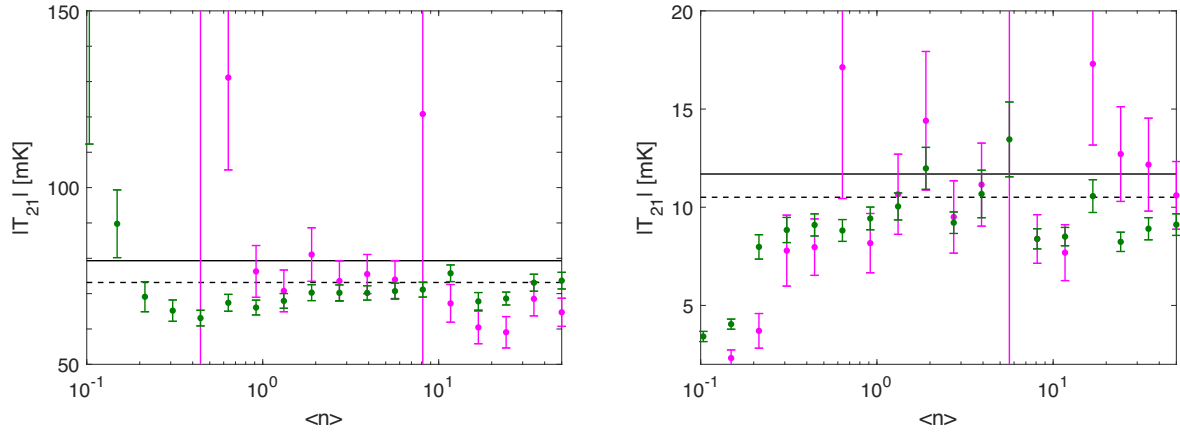


Figure 9. Extracting T_{21} with Poisson fluctuations (data points) from galaxy samples with modified values of $\langle n \rangle$ (in units of Mpc^{-3}) varied between 0.05 and 50 from a small box (128^3 , magenta) and a large box (256^3 , green) at $z = 15$ (left) and at $z = 9$ (right). At each redshift, we show the real $|T_{21}|$ (Case 2) which is constant as a function of $\langle n \rangle$ (horizontal line, solid black). For comparison, we also show $|T_{21}|$ extracted from an ideal galaxy sample (horizontal line, dashed black, large box).

signature and completely impedes parameter estimation, so that none of the quantities are measured correctly (orange data points in Fig. 8).

Next, we test the effect of the Poisson noise across the halo mass scales (assuming redshift-independent bias $b = 5$). To get a feeling of what kind of galaxy surveys would be useful, we artificially increase $\langle n \rangle$ and show the absolute value of the reconstructed temperature $T_{21}(z)$ at redshifts 14 (left) and 9 (right) versus the value of $\langle n \rangle$ in Fig. 9 for a small box (128^3 , magenta) and a large box (256^3 , green). As expected, because of the lower values of the bias at lower M_{\min} (equivalent to larger number of observed galaxies) the fitting procedure works better as we increase $\langle n \rangle$: at large $\langle n \rangle$ the data points sit close to the value of the global signal extracted using the ideal galaxy survey (horizontal dashed line). For the large box, cosmic variance is small, and Poisson fluctuations are also small as long as $\langle n \rangle$ is larger than 0.2 Mpc^{-3} . For reference, the values of $\langle n \rangle$ corresponding to $M_{\min} = 10^8$ and $M_{\min} = 10^9$ at $z = 15$ are $\langle n \rangle = 0.0211 \text{ Mpc}^{-3}$ and 0.00023 Mpc^{-3} ; and $\langle n \rangle = 0.3319 \text{ Mpc}^{-3}$ and 0.0158 Mpc^{-3} , respectively, at $z = 9$.

When planning future synergetic missions, one needs to take into account the trade-off between sample variance and Poisson noise. In Fig. 10, we show the relative errors in the brightness temperature from sample variance (blue curve and markers) and Poisson noise (black curves and markers) as a function of survey angular size. As was explained above (and demonstrated in Fig. 4), sample variance contributes statistical errors that scale as the angular size to the power of $-3/2$. It is more difficult to estimate the scaling of the Poisson errors based only on the two simulated points (extracted from the small and large simulated boxes) for each $\langle n \rangle$. To provide rough guidance, here we simply extrapolate the linear fit in $\log_{10}(\text{angular size})$ versus $\log_{10}(\Delta T/T)$. We see that small survey sizes are limited by sample variance, while on large angular scales, Poisson noise dominates even for high values of $\langle n \rangle$, i.e. low bias. However, the dependence of the Poisson error on the survey size steepens with $\langle n \rangle$ and is expected to be sub-dominant in the case of very low bias.

6 CONCLUSIONS

In this paper, we have developed a new method to measure the global spectrum using fluctuations of the 21-cm signal. The method

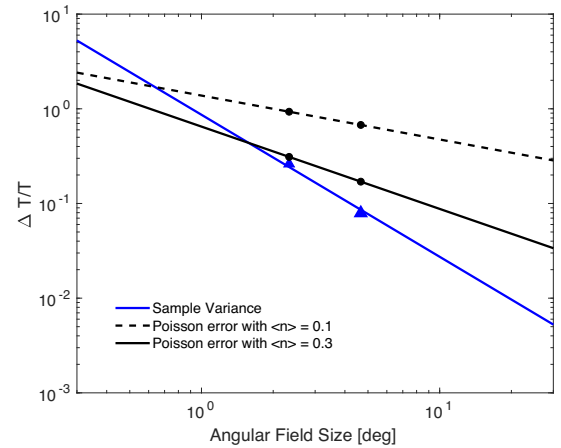


Figure 10. Trade-off between sample variance and Poisson noise at $z = 9$. The relative error in the brightness temperature ($\Delta T/T$) is shown as a function of survey angular size. The contribution from sample variance (blue solid line) scales as the survey size to the power $-3/2$, which agrees well with the measured errors (triangles indicate mean values extracted from two small (384 Mpc) and two large (768 Mpc) simulations). Black circles show the Poisson noise extracted from Fig. 9 for $\langle n \rangle = 0.1 \text{ Mpc}^{-3}$ and $\langle n \rangle = 0.3 \text{ Mpc}^{-3}$. A linear fit to these data points in $\log_{10}(\text{angular size})$ versus $\log_{10}(\Delta T/T)$ is shown with dashed and solid black lines, respectively.

is based on the multitruer technique and employs a ratio of two density fields, one of which is the Fourier transform of a 21-cm map. The second map can be of any other tracer probing the same large-scale matter density field. As a proof of concept here we used mock high-redshift galaxy surveys. In the linear regime, the ratio is anisotropic and has a well-known angular dependence. We showed that fitting the ratio as a function of the cosine of the angle with respect to the line of sight allows a measurement of large-scale properties of the two tracers such as the global 21-cm signal, window function of the dominant radiative sources that drive the signal and the galaxy bias. We test the method using both linear and non-linear theory and apply it to an ideal galaxy survey as well as to a realistic survey that contains only bright strongly biased galaxies. We use standard astrophysical scenarios to model the 21-cm signal and do not take the anomalously strong EDGES-low detection into account.

The method is reliable when applied to an ideal galaxy survey and works well both in the linear and non-linear cases allowing us to measure the global 21-cm signal and the galaxy bias. Reconstruction of the window function is more difficult in the non-linear case, although its shape and sign are recognized correctly. The shape of the window function is directly related to the spectral energy distribution of the dominant sources that drive the 21-cm signal. In the examined cases, the statistical error in the extracted window functions is small enough and allows us to discriminate between hard and soft X-ray sources responsible for cosmic heating.

We showed that at $z \lesssim 15$ the method can be applied to realistic galaxy samples featuring deep integration and a large field of view. For example, the reconstruction worked reasonably well when applied to an SKA-size survey area over which all galaxies in haloes of $10^8 M_\odot$ and above were counted (corresponding to $M_* \geq 7 \times 10^5 M_\odot$). A higher mass threshold implies a sparser and more strongly biased sample of galaxies and reduces the effectiveness of the method. Considering redshifts higher than $z \sim 15$ is not practical when applying the presented method to future galaxy surveys such as the 2000 deg² Large Area Near Infrared Survey with WFIRST which is expected to detect 1000 galaxies at $z > 10$ at the 5σ limit (and only 100 at the 10σ limit), deep observations with *JWST* that will probe much smaller solid angles and deep surveys with Euclid that will cover ~ 40 deg² with thousands of galaxies at $z > 7$.

The method can be extended and applied to other tracers of the underlying large-scale density field. For example, CO or [C II] intensity mapping of high-redshift galaxies during the EoR ($z \sim 6$ – 10 ; Moradinezhad & Keating 2018; Moradinezhad et al. 2019) is a potentially interesting candidate for such a study. Also, the population of resolved X-ray sources probed by *Lynx*, as well as the unresolved cosmic X-ray background, could play the role of the second tracer. If it is approved, *Lynx* will be sensitive to $\sim 10^4 M_\odot$ accreting black holes at redshift out to $z \sim 10$. If a wide enough survey with such an instrument turns out to be possible, the multitracers technique could be applied to the ratio of the 21-cm fluctuations and a map of X-ray sources at $z \sim 10$. On the other hand, the unresolved cosmic X-ray background could help to constrain the global spectrum of the 21-cm signal from cosmic dawn as well as to directly measure the relevant parameters of the population of X-ray binaries that heated up the IGM.

Our results are timely as more high-redshift probes are coming online, and encourage synergy between the upcoming high-redshift surveys across the entire electromagnetic spectrum. Ours is a proof-of-concept study, and further investigation is needed. First, exploring larger fields and stronger signals (in accordance with EDGES-Low) could make the method work better. Secondly, our non-linearity is only partly realistic, and a full numerical simulation will likely have more strongly non-linear fields (both 21-cm and galaxies). Finally, in this paper we assumed perfect foreground avoidance/removal, and more tests including realistic foreground treatment are required.

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APPENDIX: TECHNICAL DETAILS OF THE FITTING PROCEDURE

In the process of fitting, described in Section 4, we encountered several technical challenges:

(i) It is important to find a sweet-spot between the number of bins along the $X = \mu^2$ axis, N_X , and the number of data points per X -bin to guarantee both the smallest possible statistical errors in the estimated parameters and the good quality of the fit. We tested the convergence of the results for N_X between 5 and 150 and obtained the best results for $N_X = 50$. Because the number of samples per one X -bin is smaller at larger scales (smaller k), statistical errors are larger in $\hat{W}(k, z)$ at lower values of k .

(ii) We find that fitting the non-linear function of X in equation (8) required setting physically motivated priors and making an initial guess (within the physically motivated range) for the parameters B and A_k (while the procedure is not sensitive to the initial value of C as long as the value is positive). The fitting procedure is, therefore, performed iteratively in a few steps:

(a) We start by computing the ratio of our simulated fields (either in the linear or in the non-linear regime) for a range of k and as a function of X at a given redshift z .

(b) Fixing the value of C (we chose to always start with $C = 5$), we multiply the ratio by $(C + X)$. For every k , we fit the product with a linear function and find the y-intercept (which is our first estimate of A_k) and the slope (which gives N_k estimates for B out of which we use the mean value). These values of A_k and B are used as initial guesses at the next step. We also use the analytical calculation of $b(z)$ as the initial guess for galaxy bias when fitting the ratio in the case of a realistic galaxy sample.

(c) At the next stage, a non-linear weighted fit (weights are proportional to the number of samples per bin) is performed simultaneously for all k . $N_k + 2$ parameters are estimated, and the values of $\hat{b}(z)$ and $\hat{T}_{21}(z)$ together with σ_b and σ_T are derived. At this point, we do not save the value of $\hat{W}(k, z)$.

(d) Using the value of $C = \hat{b}(z)$ calculated above, we again multiply the ratio by $(C + X)$ and fit with a linear function to find $\hat{W}(k, z)$. We estimate the error as $\sigma_W = \sigma_{y-\text{intercept}}/\hat{T}_{21}(z)$.

At the end of this procedure, we have the best-fitting values of $\hat{b}(z)$, $\hat{T}_{21}(z)$, and $\hat{W}(k, z)$ together with $1 - \sigma$ errors in each parameter.

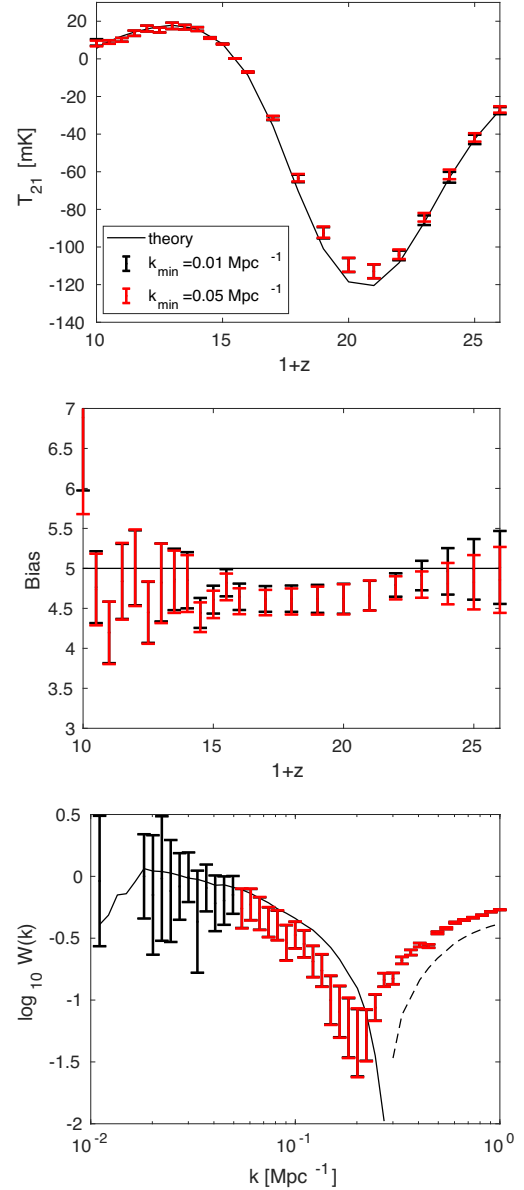


Figure A1. Robustness of the multitracer method to variations in the range of wavenumbers. Global 21-cm signal (top), galaxy bias (middle), and window function at redshift $z = 12$ (bottom) are shown for the Case 3 model. Solid/dashed lines show theoretical predictions [dashed is used only for the negative values of $W(k, z)$]; data points correspond to $k = 0.01$ – 1 Mpc^{-1} (black) and $k = 0.05$ – 1 Mpc^{-1} (red).

(iii) We have tested that the fitting procedure is robust to small changes in the range of wavenumbers. An example is shown in Fig. A1, where $\hat{T}_{21}(z)$, $\hat{b}(z)$, and $\hat{W}(k, z)$ are the results of fitting in the range $k = 0.01$ – 1 Mpc^{-1} (black) and $k = 0.05$ – 1 Mpc^{-1} (red). The agreement between the two sets of results is excellent. We find that the reconstructions of both the global signal and the galaxy bias work equally well with and without the low k modes. This test also shows that even if the lowest wavenumbers are lost to foreground subtraction, the method will work equally well as long as the higher k modes are probed with good enough precision (i.e. we still require large field of view).